

Gradual Typing for Python

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Gradual Typing

- Static and dynamic type systems have complimentary strengths.
- Static typing provides full-coverage error checking, efficient execution, and machine-checked documentation.
- Dynamic typing enables rapid development and fast adaption to changing requirements.
- Why not have both in the same language?



Java



Python

Goals for gradual typing

- Treat programs without type annotations as dynamically typed.
- Programmers may incrementally add type annotations to gradually increase static checking.
- Annotate all parameters and the type system catches all type errors.
- The type system and semantics should place a minimal implementation burden on language implementors.

Implicit coercions to/from dynamic

```
class Point:  
    def __init__(self):  
        self.x = 0  
    def move(self, dx):  
        self.x = self.x + dx
```

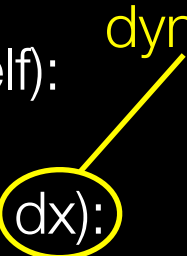
```
a = 1  
p = Point()  
p.move(a)
```

Parameters with no type annotation
are given the dynamic type.

Implicit coercions to/from dynamic

```
class Point:  
    def __init__(self):  
        self.x = 0  
    def move(self, dx):  
        self.x = self.x + dx
```

dynamic



```
a = 1  
p = Point()  
p.move(a)
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Parameters with no type annotation
are given the dynamic type.

Implicit coercions to/from dynamic

```
class Point:
    def __init__(self):
        self.x = 0
    def move(self, dx):
        self.x = self.x + dx
```

dynamic

int x int → int

```
a = 1
p = Point()
p.move(a)
```

Parameters with no type annotation
are given the dynamic type.

Implicit coercions to/from dynamic

```
class Point:
    def __init__(self):
        self.x = 0
    def move(self, dx):
        self.x = self.x + dx
```

dynamic

int x int → int

```
a = 1
p = Point()
p.move(a)
```

dynamic ⇒ int

Parameters with no type annotation
are given the dynamic type.

Implicit coercions to/from dynamic

```
class Point:
    def __init__(self):
        self.x = 0
    def move(self, dx):
        self.x = self.x + dx

int
a = 1
p = Point()
p.move(a)
```

The diagram illustrates implicit type coercion in Python. A yellow line points from the word **int** to the variable `a` in the assignment `a = 1`. Another yellow line points from the word **dynamic** to the parameter `dx` in the `move` method definition.

Parameters with no type annotation
are given the dynamic type.

Implicit coercions to/from dynamic

```
class Point:
    def __init__(self):
        self.x = 0
    def move(self, dx):
        self.x = self.x + dx

a = 1
p = Point()
p.move(a)
```

dynamic

int

int $\Rightarrow$ dynamic

Parameters with no type annotation
are given the dynamic type.

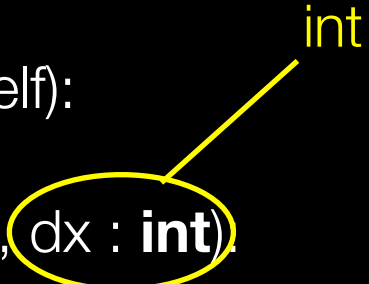
Detecting static type errors

```
class Point:  
    def __init__(self):  
        self.x = 0  
    def move(self, dx : int):  
        self.x = self.x + dx
```

```
a = 1  
p = Point()  
p.move(a)  
p.move("hi")
```

Detecting static type errors

```
class Point:  
    def __init__(self):  
        self.x = 0  
    def move(self, dx : int):  
        self.x = self.x + dx
```



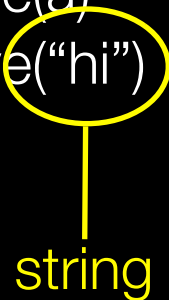
```
a = 1  
p = Point()  
p.move(a)  
p.move("hi")
```

Detecting static type errors

```
class Point:  
    def __init__(self):  
        self.x = 0  
    def move(self, dx : int):  
        self.x = self.x + dx
```



```
a = 1  
p = Point()  
p.move(a)  
p.move("hi")
```

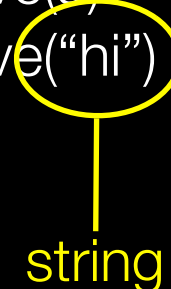


Detecting static type errors

```
class Point:  
    def __init__(self):  
        self.x = 0  
    def move(self, dx : int):  
        self.x = self.x + dx
```



```
a = 1  
p = Point()  
p.move(a)  
p.move("hi")
```



~~string $\Rightarrow$ int~~

Type System Primer

Given an expression e , a type T , and a dictionary Γ that maps variables to types, the notation

$$\Gamma \vdash e : T$$

roughly means

$$T = \text{typecheck}(\Gamma, e)$$

and the horizontal bar notation:

$$\frac{P_1 \quad P_2 \quad P_3}{Q}$$

means

$$Q \text{ if } P_1 \text{ and } P_2 \text{ and } P_3$$

Gradual Typing: replace equality with consistency ($\sim$)

$$\frac{\Gamma \vdash e_1 : \text{object}\{\dots, m : S \rightarrow T, \dots\} \quad \Gamma \vdash e_2 : S' \quad S' \sim S}{\Gamma \vdash e_1.m(e_2) : T}$$

Gradual Typing: replace equality with consistency ($\sim$)

$$\frac{\Gamma \vdash e_1 : \text{object}\{\dots, m : S \rightarrow T, \dots\} \quad \Gamma \vdash e_2 : S' \quad S' \sim S}{\Gamma \vdash e_1.m(e_2) : T}$$

The consistency relation

- Definition: a type is **consistent**, written $\sim$, with another type when they are equal in the places both are defined.
- Examples:

$\text{int} \sim \text{int}$ $\text{int} \not\sim \text{bool}$ $\text{dyn} \sim \text{int}$ $\text{int} \sim \text{dyn}$

$\text{object}\{x:\text{int} \rightarrow \text{dyn}, y:\text{dyn} \rightarrow \text{bool}\} \sim \text{object}\{y:\text{bool} \rightarrow \text{dyn}, x:\text{dyn} \rightarrow \text{bool}\}$

$\text{object}\{x:\text{int} \rightarrow \text{int}, y:\text{dyn} \rightarrow \text{bool}\} \not\sim \text{object}\{y:\text{dyn} \rightarrow \text{bool}, x:\text{bool} \rightarrow \text{int}\}$

$\text{object}\{x:\text{int} \rightarrow \text{int}, y:\text{dyn} \rightarrow \text{dyn}\} \not\sim \text{object}\{x:\text{int} \rightarrow \text{int}\}$

Consistency

$$\overline{\text{dynamic} \sim T}$$

$$\overline{T \sim \text{dynamic}}$$

$$\frac{S_1 \sim T_1 \quad S_2 \sim T_2}{S_1 \rightarrow S_2 \sim T_1 \rightarrow T_2}$$

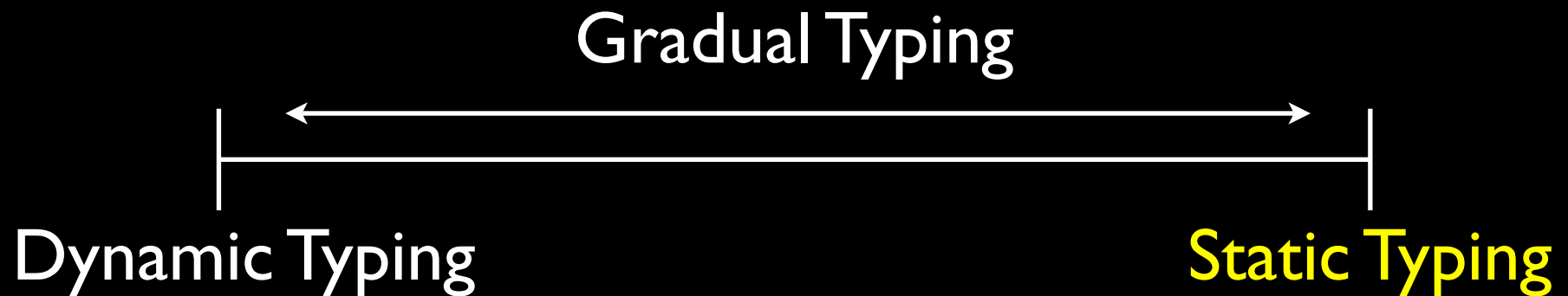
$$\text{dom}(\Gamma_1) = \text{dom}(\Gamma_2)$$

for all x in $\text{dom}(\Gamma_1)$. $\Gamma_1(x) = T_1$ and $\Gamma_2(x) = T_2$

implies $T_1 \sim T_2$

$$\overline{\text{object}\{\Gamma_1\} \sim \text{object}\{\Gamma_2\}}$$

Gradual Typing for Python



Note: type annotation syntax based on Python 3k

A Static Type System for Python

- Nominal vs. Structural Types
- Subtyping vs. Matching
- Generics with match bounds

Nominal vs. Structural

```
class Thing1:  
    def __init__(self):  
        self.x = 0  
    def move(self, dx : int):  
        self.x = self.x + dx
```

```
p = Thing1()
```

```
class Thing2:  
    def __init__(self):  
        self.x = 0  
    def move(self, dx : int):  
        self.x = self.x + dx
```

```
p = Thing2()
```

Nominal vs. Structural

```
class Thing1:  
    def __init__(self):  
        self.x = 0  
    def move(self, dx : int):  
        self.x = self.x + dx
```

p = Thing1()

|

Thing1

```
class Thing2:  
    def __init__(self):  
        self.x = 0  
    def move(self, dx : int):  
        self.x = self.x + dx
```

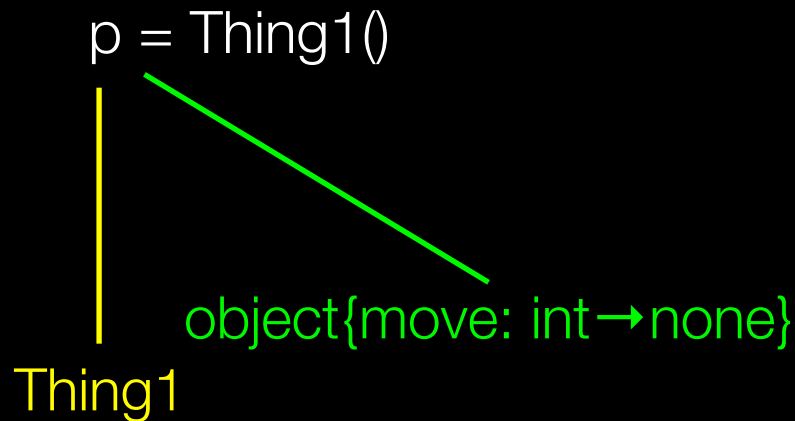
p = Thing2()

|

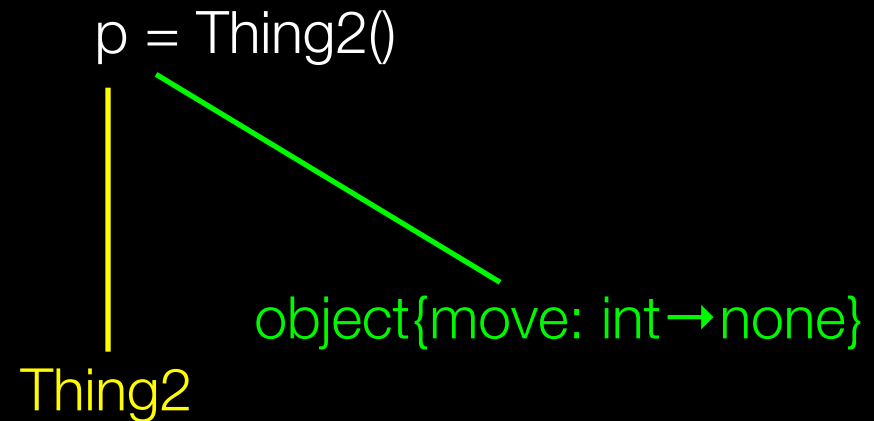
Thing2

Nominal vs. Structural

```
class Thing1:  
    def __init__(self):  
        self.x = 0  
    def move(self, dx : int):  
        self.x = self.x + dx
```



```
class Thing2:  
    def __init__(self):  
        self.x = 0  
    def move(self, dx : int):  
        self.x = self.x + dx
```



Subtyping vs. Matching

- There's two approaches to structural typing
- Structural Subtyping: thoroughly explored by Luca Cardelli and many others.
- Matching: invented by Kim Bruce, similar to OCaml's approach to objects, less well explored.

The Problem with Subtyping: Binary Methods

```
class Point:
```

```
    def __init__(self : Point):
```

```
        self.x = 0.0; self.y = 0.0
```

```
    def equal(self : Point, other : Point) -> bool:
```

```
        return x == other.x and y == other.y
```

```
class ColorPoint(Point):
```

```
    def __init__(self : ColorPoint):
```

```
        Point.__init__(self)
```

```
        self.c = 'red'
```

```
    def equal(self : ColorPoint, other : ColorPoint) -> bool:
```

```
        return Point.equal(self, other) and self.c == other.c
```

The Problem with Subtyping: Binary Methods

```
class Point:  
  def __init__(self : Point):  
    self.x = 0.0; self.y = 0.0  
  def equal(self : Point, other : Point) -> bool:  
    return x == other.x and y == other.y
```

```
class ColorPoint(Point):  
  def __init__(self : ColorPoint):  
    Point.__init__(self)  
    self.c = 'red'  
  def equal(self : ColorPoint, other : ColorPoint) -> bool:  
    return Point.equal(self, other) and self.c == other.c
```

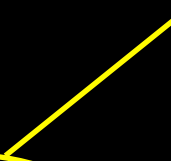
```
ColorPoint = object{__init__ : () -> ColorPoint, equal: ColorPoint -> bool }
```

The Problem with Subtyping: Binary Methods

```
class Point:  
  def __init__(self : Point):  
    self.x = 0.0; self.y = 0.0  
  def equal(self : Point, other : Point) -> bool:  
    return x == other.x and y == other.y
```

```
class ColorPoint(Point):  
  def __init__(self : ColorPoint):  
    Point.__init__(self)  
    self.c = 'red'  
  def equal(self : ColorPoint, other : ColorPoint) -> bool:  
    return Point.equal(self, other) and self.c == other.c
```

compile error,
covariance disallowed



```
ColorPoint = object{__init__ : () -> ColorPoint, equal: ColorPoint -> bool }
```

The Problem with Subtyping: Binary Methods

```
class Point:
```

```
...
```

```
class ColorPoint(Point):
```

```
....
```

```
def equal(self : ColorPoint, p : Point) -> bool:  
    other = dynamic_cast<|ColorPoint|>(p)  
    return Point.equal(self, other) and self.c == other.c
```

ew!

```
class Point3D(Point):
```

```
...
```

```
p1 = ColorPoint()
```

```
p2 = Point3D()
```

```
p1.equal(p2) // no compile error, instead get run-time error, bad!
```

Matching & Binary Methods

```
class Point:
```

```
    def __init__(self : selftype):
```

```
        self.x = 0.0; self.y = 0.0
```

```
    def equal(self : selftype, other : selftype) -> bool:
```

```
        return x == other.x and y == other.y
```

```
class ColorPoint(Point):
```

```
    def __init__(self : selftype):
```

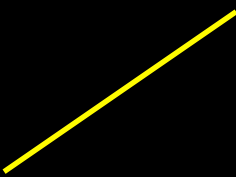
```
        Point.__init__(self)
```

```
        self.c = 'red'
```

```
    def equal(self : selftype, other : selftype) -> bool:
```

```
        return Point.equal(self, other) and self.c == other.c
```

OK!



Look Ma, no dynamic cast!

Matching & Binary Methods

```
p1 = ColorPoint()  
p2 = ColorPoint()  
p1.equal(p2) // OK!
```

```
p3 = Point3D()  
p1.equal(p3) // compile error, good!
```

Matching: Under the Hood

$$\Gamma \vdash e : T \quad T < \# \text{ object}\{m : S\}$$

$$\Gamma \vdash e.m : [\text{selftype} := T]S$$

Matching + Consistency

$$\text{dom}(\Gamma_2) \subseteq \text{dom}(\Gamma_1)$$

for all x in $\text{dom}(\Gamma_2)$. $\Gamma_2(x) = T_2$ and $\Gamma_1(x) = T_1$
implies $T_1 \sim T_2$

$$\text{object}\{\Gamma_1\} <\# \text{object}\{\Gamma_2\}$$

Generics

- Lots of Python code is polymorphic
- Generics are needed to provide enough flexibility in the type system to handle this.
- (Of course, you can always fall back on using type dynamic when you want to.)

Generic Functions

```
def pow<| T |>(f : fun(T,T), n : int) -> fun(T,T):  
  def pow_f(x : T):  
    while n > 0:  
      x = f(x); n -= 1  
    return x  
  return pow_f
```

```
def add1(x : int) -> int: return x + 1
```

```
add5 = pow<|int|>(add1, 5)
```

```
add5 = pow(add1, 5)
```

Generic Functions

```
def pow<| T |>(f : fun(T,T), n : int) -> fun(T,T):  
  def pow_f(x : T):  
    while n > 0:  
      x = f(x); n -= 1  
    return x  
  return pow_f
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def add1(x : int) -> int: return x + 1
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Generic Functions

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def pow<| T |>(f : fun(T,T), n : int) -> fun(T,T):  
  def pow_f(x : T):  
    while n > 0:  
      x = f(x); n -= 1  
    return x  
  return pow_f
```

explicit instantiation

```
def add1(x : int) -> int: return x + 1
```

```
add5 = pow<|int|>(add1, 5)
```

```
add5 = pow(add1, 5)
```

Generic Functions

```
def pow<| T |>(f : fun(T,T), n : int) -> fun(T,T):  
  def pow_f(x : T):  
    while n > 0:  
      x = f(x); n -= 1  
    return x  
  return pow_f
```

explicit instantiation

```
def add1(x : int) -> int: return x + 1
```

add5 = pow<|int|>(add1, 5)

add5 = pow(add1, 5)

implicit instantiation

Generic Classes and Methods

```
class Point<|T|>:  
    def __init__(self, x : T, y : T):  
        self.x = x; self.y = y  
  
    def map<|U|>(self, f : fun(T,U)) -> Point<|U|>:  
        return Point<|U|>(f(self.x), f(self.y))
```

```
>>> p = Point<|int|>(1, 3)  
>>> p.map(float)  
Point<|float|>(1.0, 2.0)
```

Generic Classes and Methods

```
class Point<|T|>:  
    def __init__(self, x : T, y : T):  
        self.x = x; self.y = y  
  
    def map<|U|>(self, f : fun(T,U)) -> Point<|U|>:  
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>>> p = Point<|int|>(1, 3)  
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Point<|float|>(1.0, 2.0)
```

Generic Classes and Methods

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class Point<|T|>:  
    def __init__(self, x : T, y : T):  
        self.x = x; self.y = y  
  
    def map<|U|>(self, f : fun(T,U)) -> Point<|U|>:  
        return Point<|U|>(f(self.x), f(self.y))
```

```
>>> p = Point<|int|>(1, 3)  
>>> p.map(float)  
Point<|float|>(1.0, 2.0)
```

Match-bound Generics

```
typealias Iterator = forall(T, object({next: method(selftype, T)}))
```

```
typealias Iterable = forall(T, It <# Iterator<|T|>,
                                object({__iter__: method(selftype, It) })))
```

```
def mymap<| T, R, It <# Iterable<|T|> |>( f : fun(T, R), l : It) -> list<|R|>:
  res = list<|R|>()
  for x in l: res.append(f(x))
  return res
```

```
def doubledown(a : int) -> int:
  return 2 * a
```

```
alist = [1,2,3]
mymap(doubledown, alist)
```

Match-bounds: Under the Hood

$$\frac{\Gamma \vdash e : \forall (X_1 < \# T_1, \dots, X_n < \# T_n). R \quad S_1 < \# T_1, \dots, S_n < \# T_n}{\Gamma \vdash e < |S_1, \dots, S_n| > : [X_1 := S_1, \dots, X_n := S_n] R}$$

Future Work

- Public release of the type checker
- Corpus analysis to test whether our type system is a good fit for Python programs
- Integration with Jython
- Implement run-time type checks
- Compiler optimizations to take advantage of the type information provided by gradual typing

Conclusion

- Gradual typing integrates static and dynamic typing in the same language, based on a new relation on types called consistency
- For Python, we hope a type system based on structural matching and generics will provide a good fit.
- To see a demo, find Joe during a break, or better yet, over a beer!

Why add types to a dynamic language?

- Large applications suffer from “dynamicitis”
- Values of many different kinds flow through the same point within the system. Checking code appears everywhere.
- E.g., in Django, there are places where True, ‘t’, , ‘T’, ‘True’, and I are all potential values that must be dealt with
- Annotate interfaces with types to establish invariants and document expectations

Why not ML-style inference?

- Inference alone does not provide the flexibility of dynamic typing.
- Combining inference and gradual typing may provide the best of both worlds.
- See *Gradual Typing and Unification-based Inference* by Siek and Vachharajani.